Adversarial Search

1) What is the minimax value of the root node for the game tree below? Cross out the node(s) whose value(s) the alpha-beta method never determines, assuming that it performs a depth-first search that always generates the leftmost child node first and a loss (and win) of MAX (and MIN) corresponds to a value of $-\infty$ (and ∞ , respectively). Determine the alpha and beta values of the remaining node(s).



2) Assume that you are given a version of the alpha-beta method that is able to take advantage of the information that all node values are integers that are at least 1 and at most 6. Determine ALL values for X that require the algorithm to determine the values of ALL nodes of the following game tree, assuming that the alpha-beta method performs a depth-first search that always generates the leftmost child node first.



- **3)** The minimax algorithm returns the best move for MAX under the assumption that MIN plays optimally. What happens if MIN plays suboptimally? Is it still a good idea to use the minimax algorithm?
- 4) In order to perform a move in the game a player has to roll a die. If the outcome is odd (1,3 or 5) the player has three possible moves that will reach states with utilities: 4, 5 and 10. If the outcome of the die is 2 or 4, the player has two possible moves that will reach states with utilities: 4, and 8. Finally, if the outcome of the die is 6, there are three moves that reach states with utilities 5, 7 and 9. Draw the expectiminimax tree and calculate the expectiminimax value of the root node given that:
 - a) The player is a maximum player.
 - b) The player is a minimum player.