SAT-Based Planning

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Russell and Norvig, 3rd Edition, Section 10.4.1

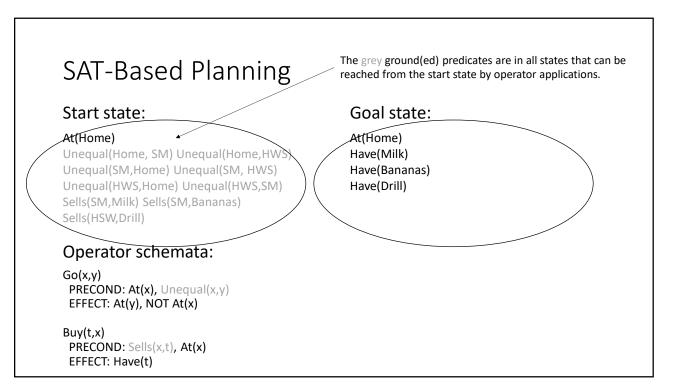
These slides are new and can contain mistakes and typos. Please report them to Sven (skoenig@usc.edu).

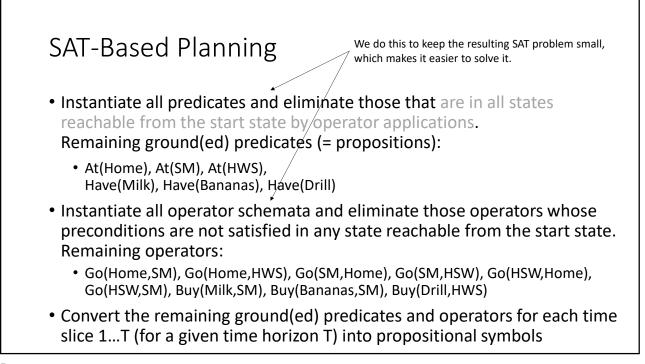
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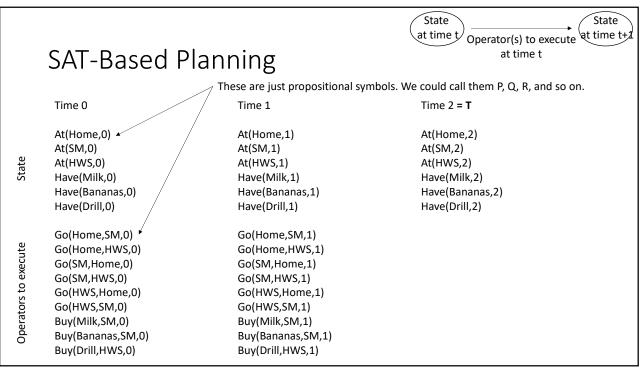
SAT-Based Planning

- Planning problem (specified in STRIPS)
- SATisfiability problem (propositional sentence)
- Solution to SATisfiability problem (interpretation that makes the propositional sentence true)
- Solution to planning problem (shortest operator sequence that transforms the start state to the goal state)

Start state:	Goal state:
At(Home)	At(Home)
Unequal(Home, SM) Unequal(Home,HWS)	Have(Milk)
Unequal(SM,Home) Unequal(SM, HWS)	Have(Bananas)
Unequal(HWS,Home) Unequal(HWS,SM)	Have(Drill)
Sells(SM,Milk) Sells(SM,Bananas)	
Sells(HSW,Drill)	
Operator schemata:	
Go(x,y)	
PRECOND: At(x), Unequal(x,y)	
EFFECT: At(y), NOT At(x)	







SAT-Based Planning

- 1. Set T := 0.
- 2. Use a SAT solver to determine truth values for all propositional symbols so that they make the conjunct of the constraints on the following slides true, where the constraints use T as a parameter and are expressed as propositional sentences that need to be true.
- 3. If the SAT solver found no solution, then set T := T+1 and go to 2.
- A plan is obtained by executing the operators whose propositional symbols are true at the corresponding time steps. For example, if Go(Home,SM,0) (≡ true) then operator Go(Home,SM) should be executed at time 0. (If no operators are executed during a time step, it can be skipped.)

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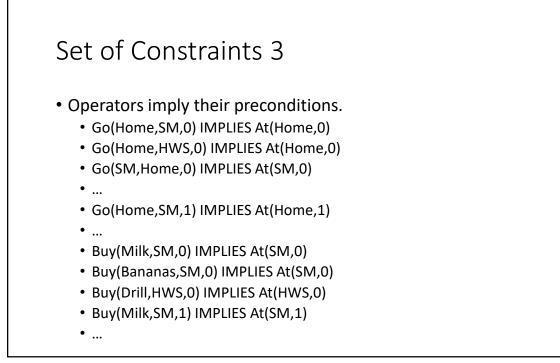
Set of Constraints 1 • The ground(ed) predicates at time 0 correspond to the start state. At(Home,0) (that is, At(Home,0) ≡ true) NOT At(SM,0) (that is, At(SM,0) ≡ false) NOT At(HWS,0) NOT Have(Milk,0) NOT Have(Bananas,0) NOT Have(Drill,0)

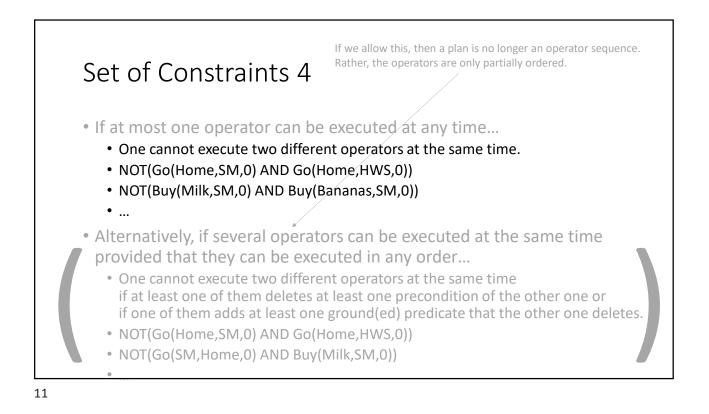
Set of Constraints 2

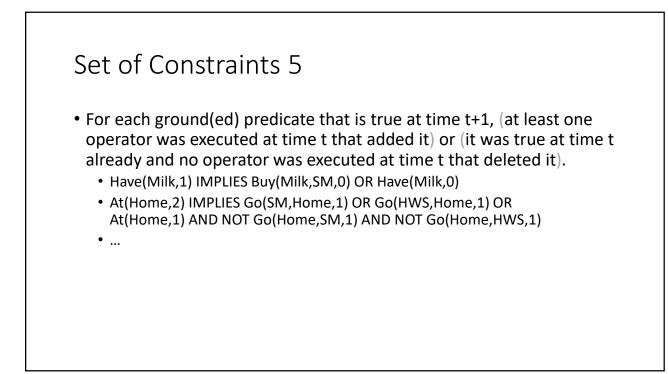
• The ground(ed) predicates at time T correspond to the goal state. If the goal state is only partially specified, then not all predicates at time T are assigned a truth value.

- At(Home,T)
- Have(Milk,T)
- Have(Bananas,T)
- Have(Drill,T)









Set of Constraints 6

- For each ground(ed) predicate that is false at time t+1, (at least one operator was executed at time t that deleted it) or (it was false at time t already and no operator was executed at time t that added it).
 - NOT Have(Milk,1) IMPLIES NOT HAVE(Milk,0) AND NOT Buy(Milk,SM,0)
 - NOT At(Home,2) IMPLIES Go(Home,SM,1) OR Go(Home,HWS,1) OR NOT At(Home,1) AND NOT Go(SM,Home,1) AND NOT Go(HWS,Home,1)

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SAT-Based Planning

- The resulting planner works well in practice.
- Issues
 - If the SAT solver is not guaranteed to find a solution even if one exists (for example, if it is based on hillclimbing with a time out), then the procedure is not guaranteed to find a shortest operator sequence.
 - If no plan exists, then the procedure will not terminate.

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