Heuristic Search

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Russell and Norvig, 3rd Edition, Sections 3.5-3.6

These slides are new and can contain mistakes and typos. Please report them to Sven (skoenig@usc.edu).

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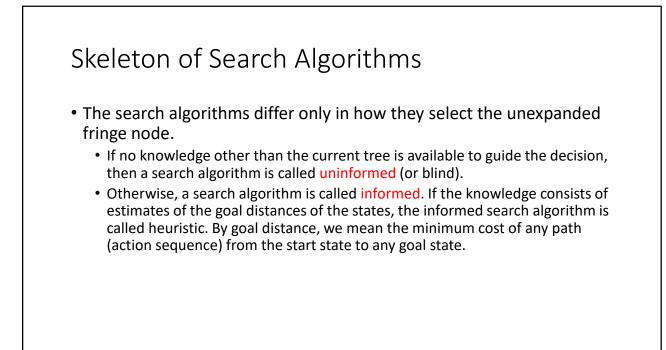
Survey

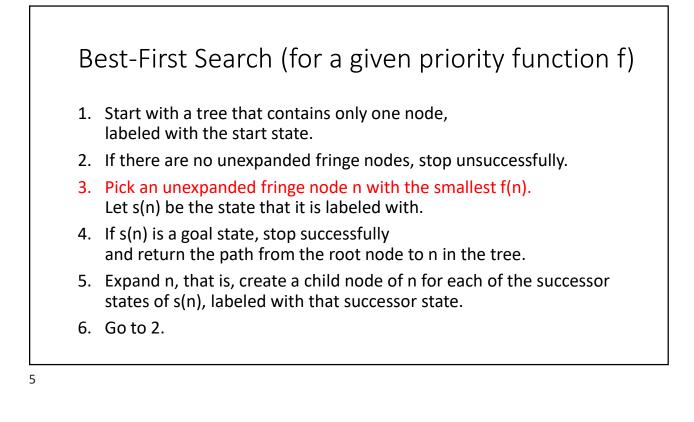
• Please respond to Jiaoyang's survey!

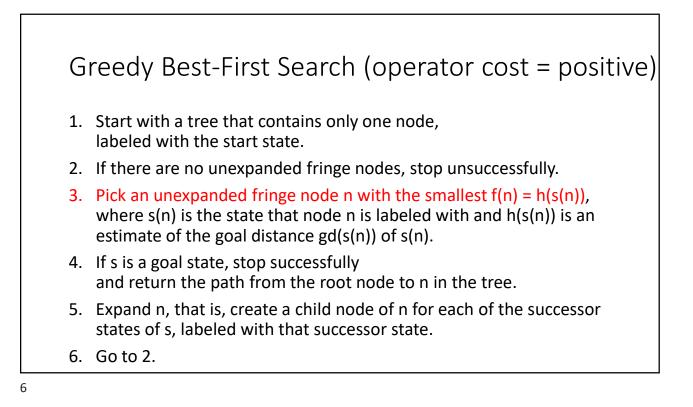
Skeleton of Search Algorithms

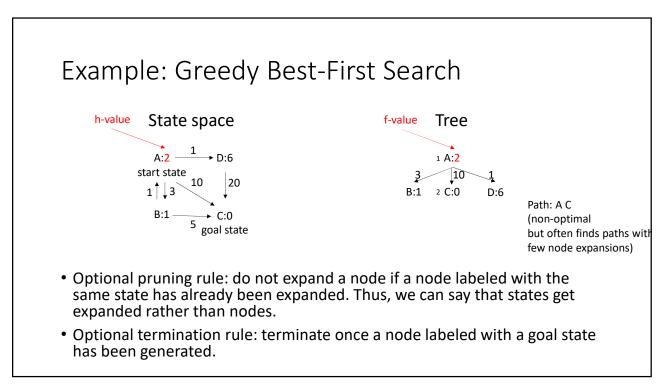
- 1. Start with a tree that contains only one node, labeled with the start state.
- 2. If there are no unexpanded fringe nodes, stop unsuccessfully.
- 3. Pick an unexpanded fringe node n. Let s(n) be the state it is labeled with.
- 4. If s(n) is a goal state, stop successfully and return the path from the root node to n in the tree.
- 5. Expand n, that is, create a child node of n for each of the successor states of s(n), labeled with that successor state.
- 6. Go to 2.

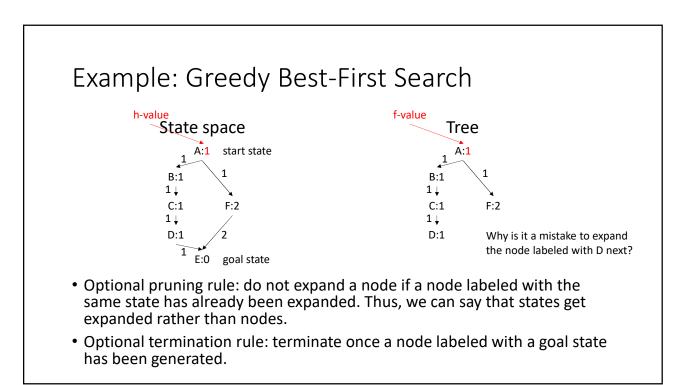


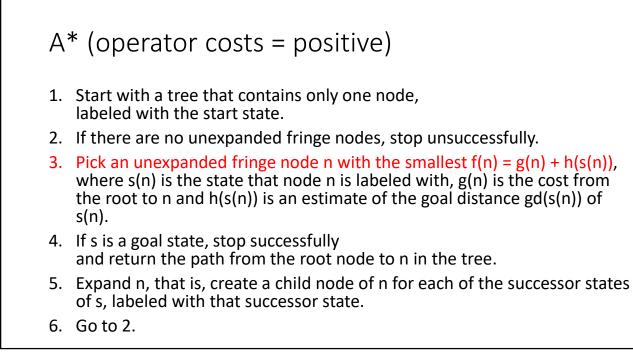






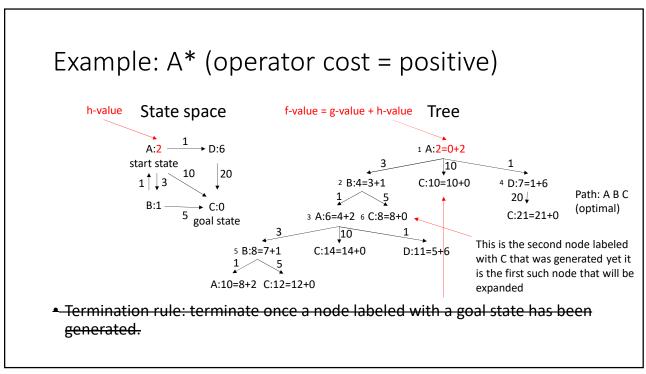




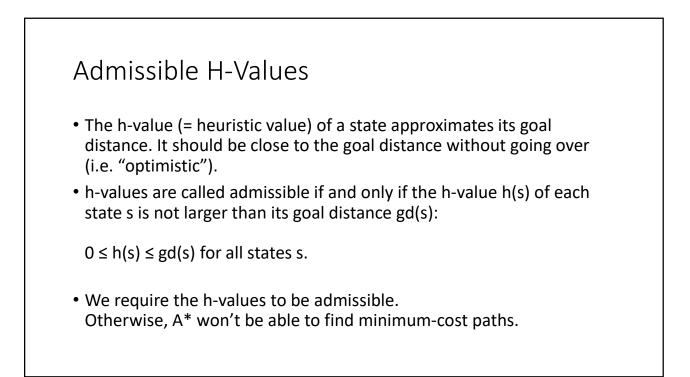


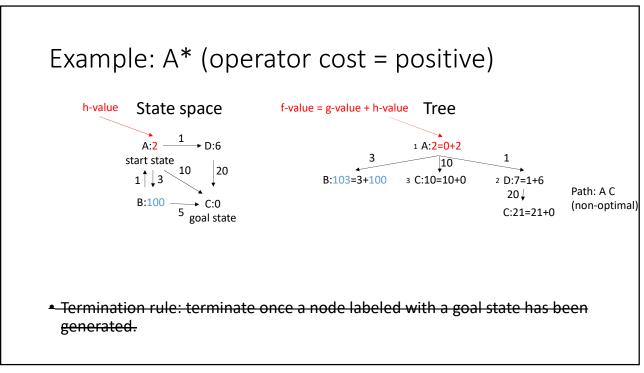
A* (operator costs = positive)

• f(n) is an estimate of the cost of a cost-minimal path from the root node (start state) along the tree to node n and from there to any goal state.

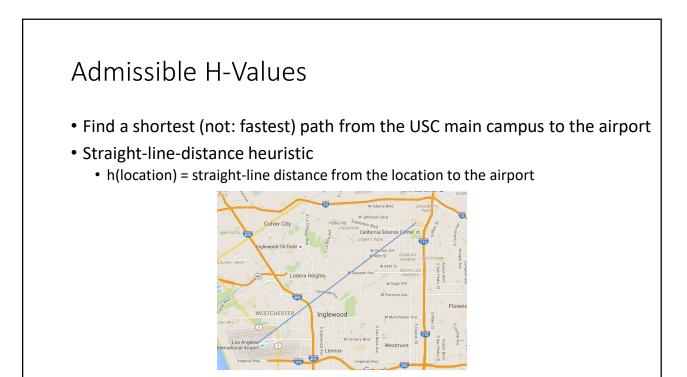


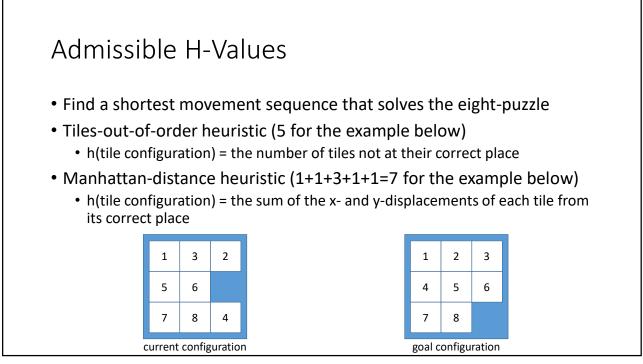


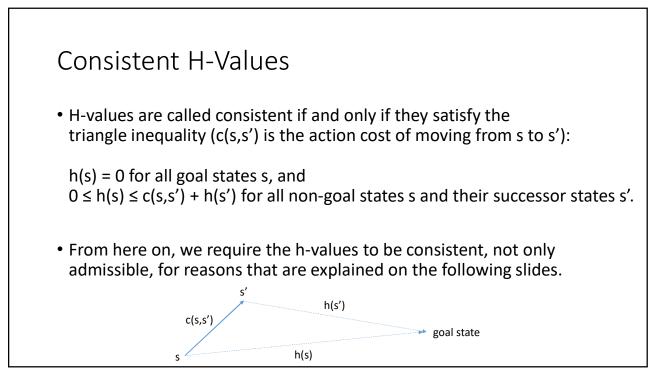


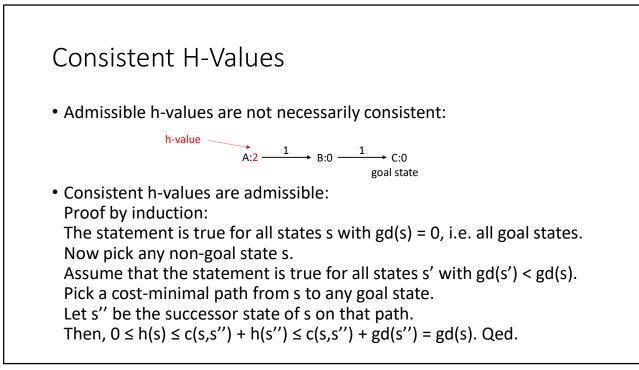


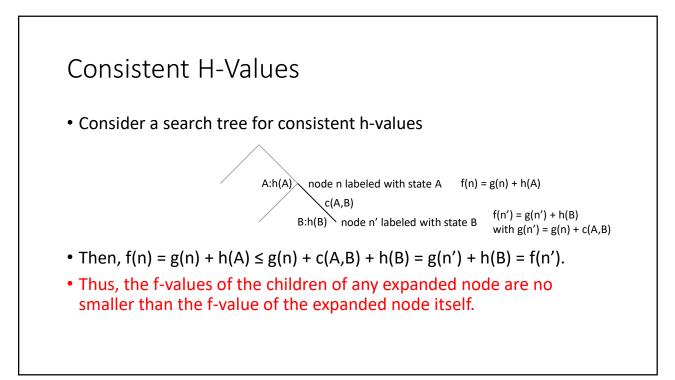












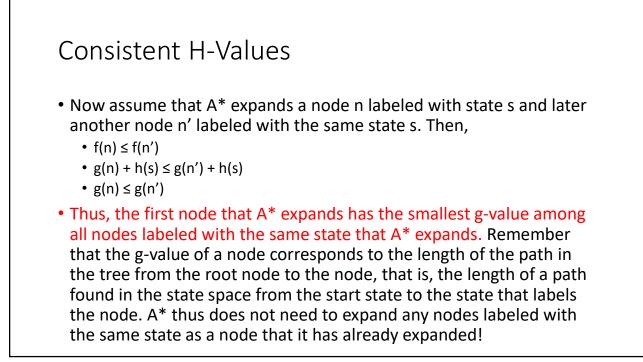
Consistent H-Values

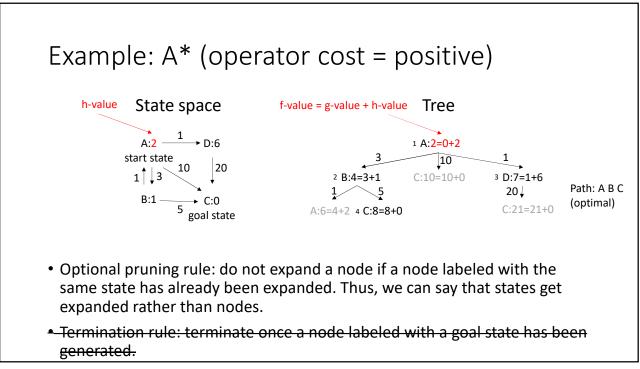
- Assume that A* picks node n for expansion and that the set of unexpanded fringe nodes at this point in time is OPEN. Then, the fvalues of all nodes in OPEN are no smaller than the f-value of node n since A* always picks an unexpanded fringe node with the smallest fvalue for expansion (Property A).
- Assume that the set of children of node n after its expansion is C. The f-values of the children of node n are no smaller than the f-value of node n (Property B), see the previous slide.
- (Our argument continues on the next slide...)

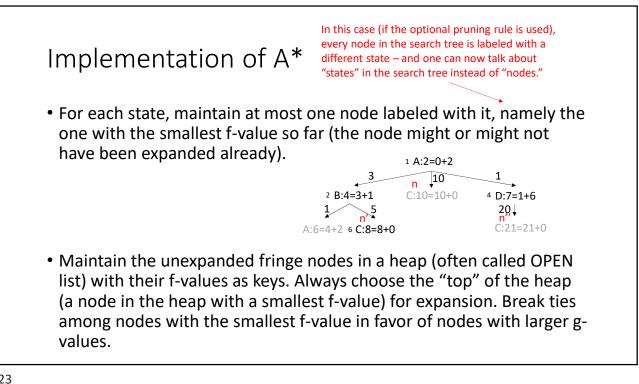
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Consistent H-Values

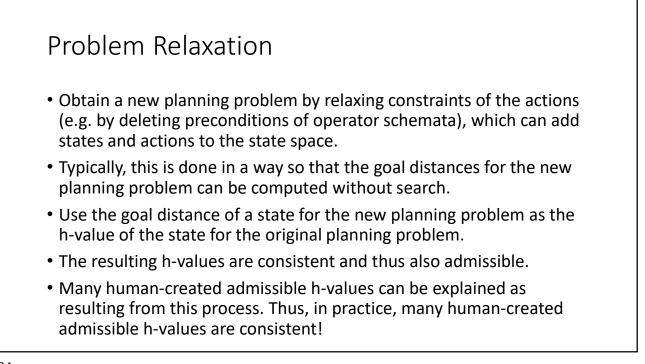
- After the expansion of node n, the new set of unexpanded fringe nodes is OPEN' := (OPEN\{n})UC since node n is no longer an unexpanded fringe node but the children of node n have become new unexpanded fringe nodes.
- A* must pick one of the nodes in OPEN' for the next expansion, and the f-values of all nodes in OPEN' are no smaller than the f-value of node n according to (Property A) and (Property B).
- Thus, A* expands nodes in order of non-decreasing f-values. That is, a node that A* expands later than some other node has an f-value that is no smaller than the f-value of the other node.





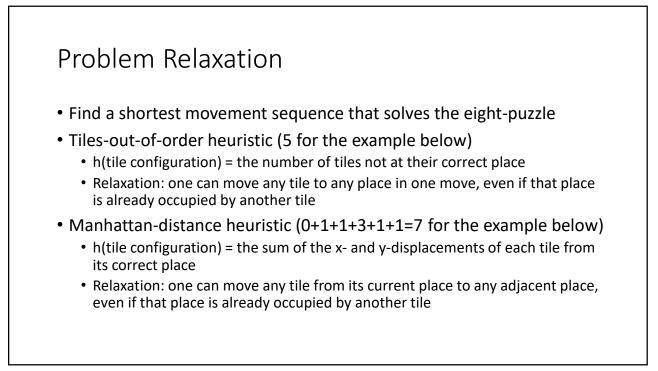


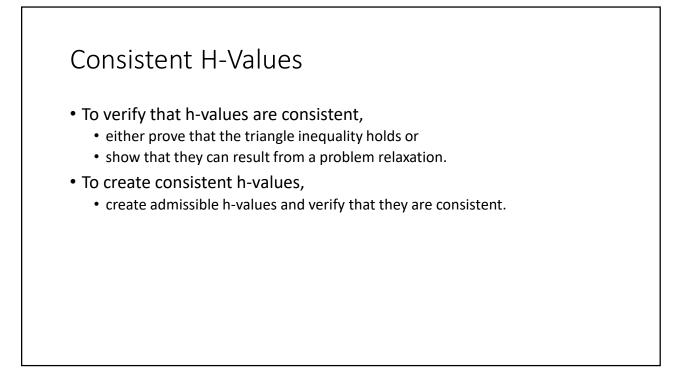




Problem Relaxation Find a shortest (not: fastest) path from the USC main campus to the airport Straight-line-distance heuristic h(location) = straight-line distance from the location to the airport Relaxation: one can drive on- and off-roads

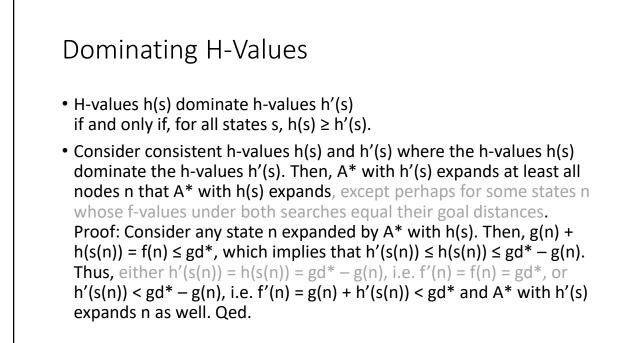






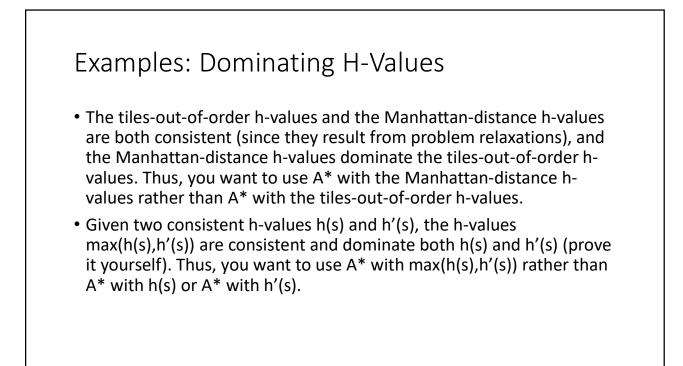
Dominating H-Values

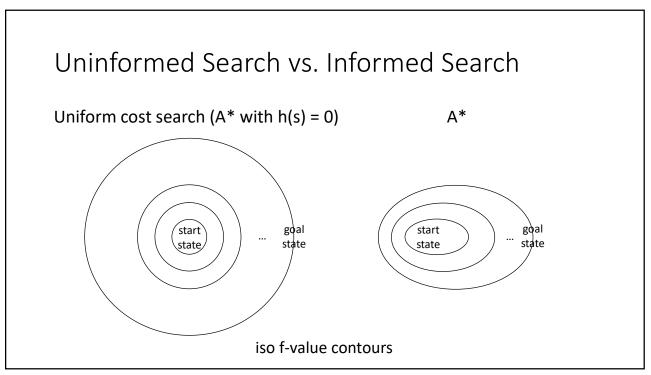
- A* expands nodes in order of non-decreasing f-values. Let gd* be the goal distance of the start state or, equivalently, the g-value and f-value of the node labeled with a goal state that A* is about to expand when it terminates. Then, A* expands
 - all nodes n with f(n) < gd*, and
 - no nodes n with f(n) > gd*.

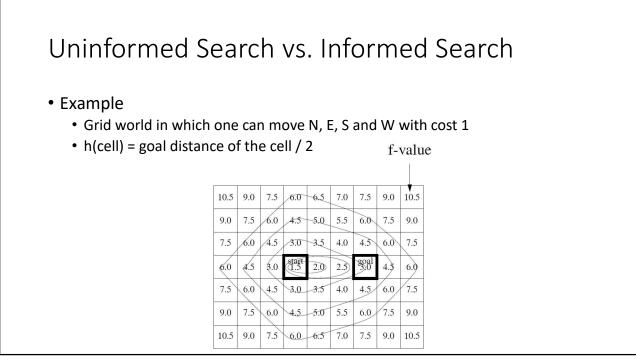


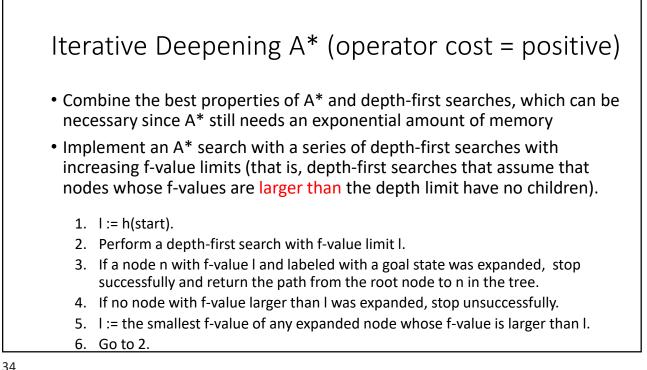
Dominating H-Values

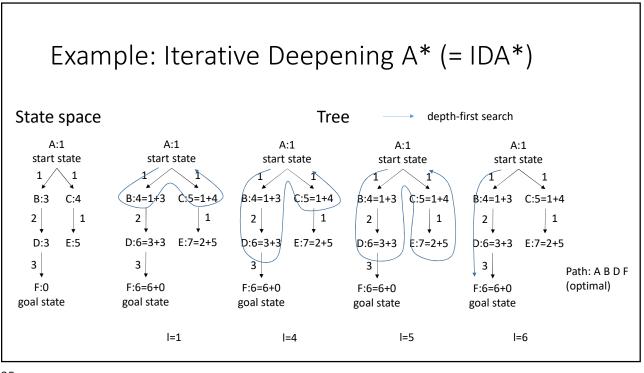
- Given consistent h-values h(s) and h'(s) where the h-values h(s) dominate the h-values h'(s). Then, A* with h'(s) and A* with h(s) both find cost-minimal paths but A* with h(s) runs at least as fast (in terms of node expansions) as A* with h'(s), perhaps up to tie-breaking among nodes whose f-values equal their goal distances.
- Note: This does not take into account that calculating the h-values h(s) and h'(s) can take different amounts of time!











Example: Iterative Deepening A* (= IDA*) The overhead of Iterative Deepening over Breadth-First Search (i.e. the percentage of additional node expansions) is often smaller than the overhead of Iterative Deepening A* over A*. The reason is that there are often more nodes with the same g-value [= all of them get expanded for the first time during the same Depth-First Search of Iterative Deepening] when all action costs are one than there are nodes with the same f-value [= all of them get expanded for the first Search of Iterative Deepening] when all action costs are one than there are nodes with the same f-value [= all of them get expanded for the first time during the same Depth-First Search of Iterative Deepening A*] (especially when all action costs are different).

Heuristic Search

- Want to play around with heuristic search algorithms?
- Go here: <u>http://aispace.org/search/</u>